|              |   |                |                 |                  |                   |          | _        |            |                   |
|--------------|---|----------------|-----------------|------------------|-------------------|----------|----------|------------|-------------------|
| E            | Entrance Examination for Admission to the P.G. Courses in the<br>Teaching Departments, 2024 |                |                 |                  |                   |          |          |            | 16                |
|              | CSS   |                |                 |                  |                   |          |          |            |                   |
|              | MA  | THEM.<br>FINAI | ATICS<br>NCE AI | / MATH<br>ND COI | IEMAT<br>MPUTA    | ICS WI   | тн       |            |                   |
|              |   |                |                 |                  |                   |          |          |            |                   |
|              |   |                | Gener           | al Instru        | <u>ctions</u>     |          |          |            |                   |
| а <u>т</u> і |   |                | 400.0           |                  | <u> </u>          |          |          |            |                   |
| 1. IN        | e Question Papel  | r is navin     | ig 100 O        | bjective         | Question          | is, each | carrying | one ma     | rĸ.               |
| 2. Th        | e answers are to  | be (✔) 't      | ick mark        | ed' <b>only</b>  | in the " <b>F</b> | Respons  | se Sheet | t" provide | ed.               |
| 3. <u>Ne</u> | gative marking  | : 0.25 ma      | arks will       | be dedu          | cted for          | each wro | ong ansv | ver.       |                   |
| Time : 2     | Hours   |                |                 |                  |                   |          | Ν        | /lax. Mai  | r <b>ks : 100</b> |
| To be f      | lled in by the Ca   | ndidate        |                 |                  |                   |          |          |            |                   |
| Registe      | r in Figures  |                |                 |                  |                   |          |          |            |                   |
| Numbe        | in words  |                |                 |                  |                   |          |          |            |                   |
|              |   |                |                 |                  |                   |          |          |            |                   |
|              |   |                |                 |                  |                   |          |          |            |                   |

Choose appropriate answer from the options in the questions.

(100 × 1 = 100 marks)

Code No. **T – 2126** 

- 1. Let  $f : \mathbb{R} \to \mathbb{R}$  defined by  $f(x) = \min\{x, x+1, |x-2|\}$ . Then
  - A. *f* decreases on the interval  $(-\infty, 1]$
  - B. *f* is not continuous on  $\mathbb{R}$
  - C. *f* is not differentiable at exactly two points
  - D. f increases on the interval [1, 2]

DONOTWRITEHERE

- 2. Let  $f:[0,1] \to \mathbb{R}$  be defined by  $f(x) = \begin{cases} 1 & \text{if } x = 1/4, \\ 2 & \text{if } x = 1/2 \\ 0 & \text{if } x \in [0,1] \setminus \{1/2, 1/4\} \end{cases}$ 
  - A. *f* is Riemann integrable and  $\int_{0}^{1} f(x) dx = 0$
  - B. f is not Riemann integrable

C. *f* is Riemann integrable and 
$$\int_{0}^{1} f(x) dx = 2$$

D. *f* is Riemann integrable and  $\int_{0}^{1} f(x) dx = 1$ 

| 3. | Whi         | ch one of the following does not im                               | ply a         | e = 0 ?                                       |
|----|-------------|---|---------------|---|
|    | Α.          | for every $\in > 0, 0 \le a \le $                                 | В.            | for every $\in > 0$ , $a < \in$               |
|    | C.          | for every $\in > 0, 0 \le a \le \in$                              | D.            | for every $\in > 0, -\epsilon < a < \epsilon$ |
| 4. | An<br>ratio | algebraic number is a root o<br>nal. The set of algebraic numbers | f a<br>is     | polynomial whose coefficients are             |
|    | Α.          | uncountable   | В.            | countably infinite                            |
|    | C.          | finite  | D.            | none of these                                 |
| 5. | The         | limit of the sequence $(\sqrt{(n+1)(n+1)})$                       | <u>2)</u> – n | ) is  |
|    | Α.          | 3   | В.            | 3/2   |
|    | C.          | 0   | D.            | $\sqrt{2} - 1$                                |
| 6. | The         | sequence $\left(\frac{2^{n+1}+3^{n+1}}{2^n+3^n}\right)$ converge  | s to          |   |
|    | A.          | 0   | В.            | 1   |
|    | C.          | 3   | D.            | 2   |
| 7. | The         | value of the integral $\int_{-\infty}^{\infty} e^{-x^2} dx$ is    |               |   |
|    | A.          | $\sqrt{\pi}$  | В.            | $2\sqrt{\pi}$                                 |
|    | C.          | 0   | D.            | $\sqrt{\pi}/2$                                |
| 8. | If $\Sigma$ | $a_n = a$ and $\sum  a_n  = b$ , and $a$ and $b$                  | are fi        | nite, then                                    |
|    | Α.          | a = b   | В.            | a≤b   |
|    | C.          | a  = b  | D.            | $a \ge b$                                     |
| 9. | lf x,       | $n_{n} = 1 + (-1)^{n} + \frac{1}{3^{n}}$ , then                   |               |   |
|    | Α.          | lim sup $x_n \neq \lim \inf x_n$                                  | В.            | $\liminf x_n = -1$                            |
|    | C.          | $x_n$ is a convergent sequence                                    | D.            | $\limsup x_n = 1$                             |

10. Let  $(x_n)$  be a sequence defined by  $x_1 = 2$  and  $x_{n+1} = \frac{1}{2} \left( x_n + \frac{2}{x_n} \right)$ . Then

- A.  $(x_n)$  is an increasing sequence
- B.  $(x_n)$  converges to  $2\sqrt{2}$
- C.  $(x_n)$  converges to a rational number
- D.  $(x_n)$  is a decreasing sequence
- 11. For  $x \in \mathbb{R}$ , let [x] denote the greatest integer *n* such that  $n \le x$ . The function x[x] is
  - A. continuous everywhere B. continuous if  $x \in \mathbb{R} \setminus \mathbb{Z}$
  - C. continuous only at  $x = \pm 1, \pm 2,...$  D. bounded on  $\mathbb{R}$
- 12. The subset  $A = \{x \in \mathbb{Q} : -1 < x < 0\} \cup \mathbb{N}$  of  $\mathbb{R}$  is
  - A. bounded, infinite set and has a limit point in  $\mathbb{R}$
  - B. unbounded, infinite set and has a limit point in  $\mathbb{R}$
  - C. unbounded, infinite set and does not have a limit point in  $\mathbb{R}$
  - D. bounded, infinite set and does not have a limit point in  $\mathbb{R}$
- 13. The sequence of real-valued functions  $f_n(x) = x^n$ ,  $x \in [0, 1] \cup \{2\}$ , is
  - A. uniformly convergent
  - B. not bounded
  - C. pointwise convergent but not uniformly convergent
  - D. bounded but not pointwise convergent

| 14. | The | series $\sum_{n=1}^{\infty} \frac{(2n)!}{(n!)^2}$ is |    |                  |  |
|-----|-----|--|----|------------------|--|
|     | Α.  | converges to 1                                       | В. | converges to 1/2 |  |
|     | C.  | converges to e                                       | D. | divergent        |  |

15. If  $(x_n)$  be a sequence such that  $x_n \ge 0$  for every  $n \in \mathbb{N}$  and if  $\lim_{n \to \infty} (-1)^n x_n$  exists then which one of the following statements is true?

- A. The sequence  $(x_n)$  is divergent
- B. The sequence  $(x_n)$  is unbounded
- C. The sequence  $(x_n)$  is not a Cauchy sequence
- D. The sequence  $(x_n)$  is a Cauchy sequence

16. For the function  $f(x) = \frac{\sin x}{x^2}$ , how many points exist in the interval  $[0, 7\pi]$  such that f'(c) = 0

- 17. The function  $f(x) = x^4 6x^2$  is increasing on the intervals
  - A.  $(-\infty, -\sqrt{3})$  and  $(0, \sqrt{3})$  onlyB.  $(\sqrt{3}, \infty)$  onlyC.  $(0, \sqrt{3})$  onlyD.  $(-\sqrt{3}, 0)$  and  $(\sqrt{3}, \infty)$  only

18. The value of the double integral  $\int_{0}^{1} \int_{0}^{x^{2}} e^{y/x} dx dy$  is A. 0 B. 1/2

C. -1/2 D. e

- 19. The value of the triple integral  $\int_{0}^{x/2 \sin \theta} \int_{0}^{r} r \, dr \, d\theta \, dz$  is A. 1/4 B. 1/2
  - C. 0 D. –1

20. The area of the region in the first quadrant enclosed by the graphs of  $x = y^2$  and x = y + 2 is

A.9B.3/2C.9/2D.3

21. If *C* is the circle  $x^2 + y^2 = 1$  taken in anticlockwise rotation, then the value of the integral  $\int_C (x^{2024} y^{2025} + 2025y) dx + (x^{2025} y^{2024} + 2024x) dy$  is

| Α. | $\pi$   | В. | 2π |
|----|---------|----|----|
| C. | $\pi/2$ | D. | 0  |

22. Consider a closed surface *S* surrounding volume *V*. If  $\vec{r}$  is the position vector of *a* point inside *S*, with the unit outward normal  $\vec{n}$  on *S*, then the value of the integral  $\iint 5\vec{r} \cdot \vec{n} dS$  is

| Α. | 5 <i>V</i> | В. | V   |
|----|------------|----|-----|
| C. | 0          | D. | 15V |

23. For what value of c does the line  $\frac{x}{2} = \frac{y}{c} = \frac{z}{3}$  lie in the plane x + 3y + 5z = 0?

- A. -13/3 B. 17/3 C. 13/3 D. -17/3
- 24. The surface  $xyz + 2yz + x^2 = 19$  has a normal line *T* at *P* = (1, 2, 3). Then T meets the x y plane at point Q which is
  - A. (8, 9, 6) C. (6, 5, 0) B. (-3, -5/2, 0) D. (3, 5/2, 0)

25. Let  $x(u,v) = ue^{u} + v$  and  $y(u,v) = ve^{2u}$ . Then the Jacobian  $\frac{J(x,y)}{J(u,v)}$  at u = 1, v = 0 is A. eC.  $e^{2}$ D.  $2e^{3}$ 

26. Consider the line integral  $\int_{C} (2x+y)dx + (x+z)dy + (y-2z)dz$  where *C* is some curve joining the points A = (0, 0, 0) and B = (1, 5, 5). The value of the integral is A. -18 B. 6 C. 56 D. 32

27. Let *F* denote a vector field and let *f* define a scalar function of three variables. Which of the following expressions is a meaningful expression?

| Α. | div (div <i>F</i> )  | В. | grad (grad <i>F</i> ) |
|----|----------------------|----|-----------------------|
| C. | curl(curl <i>F</i> ) | D. | grad (grad <i>f</i> ) |

- 28. The equations of the lines joining the vertex of the parabola  $y^2 = 6x$  to the points on it which have abscissa 24 are
  - A.  $2y \pm x = 0$  B.  $2x \pm y = 0$
  - C.  $x \pm 2y = 0$  D.  $y \pm x = 0$

29. Find the inverse Laplace transform of the function  $\frac{3}{(s+1)^3}$ 

- A.  $(3/2)t^2e^t$  B.  $3t^2e^{-t}$
- C.  $(3/2)t^2e^{-t}$  D.  $t^2e^{-t}$

30. The center of the ring of  $2 \times 2$  matrices over  $\mathbb{R}$ 

A. 
$$\left\{ \begin{pmatrix} 0 & a \\ b & 0 \end{pmatrix} : a, b \in \mathbb{R} \right\}$$
  
B. 
$$\left\{ \begin{pmatrix} 0 & a \\ a & 0 \end{pmatrix} : a \in \mathbb{R} \right\}$$
  
C. 
$$\left\{ \begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix} : a, b \in \mathbb{R} \right\}$$
  
D. 
$$\left\{ \begin{pmatrix} a & 0 \\ 0 & a \end{pmatrix} : a \in \mathbb{R} \right\}$$

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- 31. The set of units of the Gaussian ring  $z[i] = \{a + ib : a, b \in \mathbb{Z}\}$  is
  - A.  $i \mathbb{Z}$ B.  $\mathbb{Z}$ C.  $\mathbb{Z} \cup i \mathbb{Z}$ D.  $\{\pm 1, \pm i\}$
- 32. Group of automorphisms of  $\mathbb{Z}_{10}$  is isomorphic to
  - A.  $\mathbb{Z}_2 \times \mathbb{Z}_2$  B.  $\mathbb{Z}_4$
  - C.  $\mathbb{Z}_{10}$  D.  $\mathbb{Z}_2$
- 33. The system of equations  $6x_1 2x_2 + 2\alpha x_3 = 1$  and  $3x_1 x_2 + x_3 = 5$  has no solution if  $\alpha$  is equal to
  - A. 1 B. -5 C. 5 D. -1
- 34. Let *G* be a group of order 6. Then
  - A. *G* is abelian but not cyclic
  - B. G is cyclic
  - C. there is not sufficient information to determine G
  - D. G has 2 possibilities (upto isomorphism)
- 35. The number of group homomorphisms from  $\mathbb{Z}_{12}$  to  $\mathbb{Z}_{13}$  is
  - A. 0 B. 1 C. 2 D. 3
- 36. Let *G* be a group and *H* be a subgroup of *G*. Which of the following statements is true?
  - A. If *H* is a normal subgroup of *G* then gH = Hg for all  $g \in G$
  - B. If *H* is a normal subgroup of *G* then  $gH \neq Hg$  for all  $g \in G$
  - C. If  $gH \neq Hg$ , for some  $g \in G$  then H is a normal subgroup of G
  - D. If gH = Hg, for some  $g \in G$  then *H* is a normal subgroup of *G*

- 37. Which of the following statements are true?
  - every group of order 4 is cyclic Α.
  - Β. every group of order 6 is abelian
  - C. every subgroup of a cyclic group is cyclic
  - every group of order 6 is cyclic D.
- 38. The smallest non abelian group is
  - Α. Β. Klein 4 group  $S_3$
  - C. D.  $D_{4}$  $\mathbb{Z}_4$
- 39. In the Klien 4 group
  - Α. order of every element except identity is 2
  - Β. order of every element is 2
  - C. order of every element except identity is 3
  - D. order of every element except identity is 4

#### 40. The infinite cyclic group $\mathbb{Z}$ has exactly

- Α. five generators Β. two generators
- C. one generator D. three generators

41. The number group homomorphisms from  $\mathbb{Z}_{25} \to \mathbb{Z}$  is

- Α. 3 2 Β. C. 4 1
- D.

42. The number of ring homomorphisms from  $\mathbb{Z}$  to  $\mathbb{Z}$  is

- Α. 2 B. 0
- C. 1 infinite D.
- 43. In a division ring there are exactly
  - Α. only one idempotent B. two idempotents
  - C. four idempotents D. three idempotents

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44. If *p* is a prime number,  $x^p + a$  is irreducible over  $\mathbb{Z}_p[x]$ 

- A. for some values of  $a \in \mathbb{Z}_p$  B. exactly two values of  $a \in \mathbb{Z}_p$
- C. exactly one value of  $a \in \mathbb{Z}_p$  D. for all  $a \in \mathbb{Z}_p$

45. The polynomial  $f(x) = x^2 + 8x - 2$  is

- A. irreducible over  $\mathbb{Q}$  B. irreducible over  $\mathbb{R}$
- C. reducible over  $\mathbb{R}$  D. irreducible over  $\mathbb{Q}$  and  $\mathbb{R}$
- 46. Which of the following statements are true?
  - A.  $\{0, 2, 4\}$  is a prime but not a maximal ideal of  $\mathbb{Z}_6$
  - B.  $\{0, 2, 4\}$  is not an ideal of  $\mathbb{Z}_6$
  - C.  $\{0, 2, 4\}$  is a prime and a maximal ideal of  $\mathbb{Z}_6$
  - D.  $\{0, 2, 4\}$  is not a prime but a maximal ideal of  $\mathbb{Z}_6$

47. 
$$\frac{\mathbb{Z}_{3}[x]}{\langle x^{3} + c \rangle}$$
 is not a field if  
A.  $c = 2$   
C.  $c = 1$   
B.  $c = 3$   
D.  $c = 0$ 

- 48. The number of diagonal  $3 \times 3$  complex matrices A such that  $A^3 = I$  is
  - A. 9 B. 27 C. 3 D. 1
- 49. Let  $T: \mathbb{R}^3 \to \mathbb{R}^3$  be the linear transformation defined by  $T(x_1, x_2, x_3) = (x_1 + x_2, x_2 + x_3, x_3 + x_1)$ . Then an eigenvalue of T is A. 0 B. 3 C. 4 D. 2

- 50. The solutions  $x^2y'' + xy' + 4y = 0$  are
  - $\cos(4\log x)$ ,  $\sin(4\log x)$ B.  $\cos(\log x)$ ,  $\sin(\log x)$ Α.
  - $\cos(2\log x)$ ,  $\sin(2\log x)$  $\cos(\log x)$ ,  $\sin(2\log x)$ C. D.

51. An integrating factor of the differential equation  $(y^2x - x^2y)dx + x^3dy = 0$  is

- B.  $(xy)^{-2}$ (xy)Α.
- C.  $(xy)^{-1}$

52. The derivative of the function  $y = \sin^{-1}\left(\sqrt{\frac{x-1}{x+1}}\right) + \sec^{-1}\left(\sqrt{\frac{x+1}{x-1}}\right)$  is 2 Α. Β. 1

- 0 C. 3 D.
- 53. The distinct eigenvalues of the matrix  $\begin{pmatrix} 1 & 1 & 0 \\ 1 & 1 & 0 \\ \end{pmatrix}$  are B. 1, 2 A. 0, -1 C. 0, 1 D. 0, 2

54. If -1, 2,3 are the eigenvalues of a  $3 \times 3$  matrix, then its determinant is

- 0 A. Β. 4 C. -6 D. 6
- 55. The dimension of the vector space  $\mathbb{R}$  over  $\mathbb{Q}$  is
  - Α. 0 Β. infinite C.
    - 1 D. 2

- D.  $(xy)^{-3}$

56. Consider the following subsets of the vector space  $\mathbb{R}^2$ :

S1:  $\{(x, y): x + y \ge 0\}$ 

S2:  $\{(x, y): x^2 + y^2 \ge 1\}$ 

Which of the following statements are true?

- A. S1 is not a subspace but S2 is a subspace
- B. neither S1 nor S2 is a subspace of  $\mathbb{R}^2$
- C. S1 is a subspace but S2 is not a subspace
- D. both S1 and S2 are subspaces of  $\mathbb{R}^2$
- 57. If  $V_1$  and  $V_2$  are 3-dimensional subspaces of *a* 4 dimensional vector space *V*, then the smallest possible dimension of  $V_1 \cap V_2$  is

| A. | 3 | В. | 1 |
|----|---|----|---|
| C. | 2 | D. | 4 |

- 58. Let *W* be the vector space of all symmetric matrices over  $\mathbb{R}$ . Then the dimension of *W* is
  - A. 3 B. 1 C. 2 D. 0

59. The  $10 \times 10$  matrix with all entries 1 have rank

- A. 10
   B. 0

   C. 1
   D. 2
- 60. A consistent linear system of two equations in two unknowns has
  - A. Exactly one solution
  - B. Infinitely many solutions
  - C. Exactly one solution or an infinite number of solutions
  - D. Exactly two solutions

61. Let  $A = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix}$  be such that A has real eigenvalues. Then

A. 
$$\theta = 0, \frac{-\pi}{2}$$
 B.  $\theta = 0, \frac{-3\pi}{2}$ 

C. 
$$\theta = 0, \pi$$
 D.  $\theta = 0, \frac{\pi}{2}$ 

62. A homogeneous system of 5 linear equations in 6 variables admits

- A. Finite, but more than 2 solutions in  $\mathbb{R}^6$
- B. No solution in  $\mathbb{R}^6$
- C. Infinitely many solutions in  $\mathbb{R}^6$
- D. A unique solution in  $\mathbb{R}^6$

63. Suppose the matrix  $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$  has an eigenvalue 1 with associated eigenvector  $x = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$ . What is  $A^{50}x$ ? A.  $\begin{bmatrix} 2 \\ 3 \end{bmatrix}$ C.  $\begin{bmatrix} a & b \\ c & d \end{bmatrix}$ B.  $\begin{bmatrix} 2^{50} \\ 3^{50} \end{bmatrix}$ D.  $\begin{bmatrix} a^{50} & b^{50} \\ c^{50} & d^{50} \end{bmatrix}$ 

64. Given that a 3 × 3 matrix satisfies the equation  $A^3 - A^2 + A - I = 0$ . Then the value of  $A^4$  is

A. 
$$-A^3 - A^2 + A - I = 0$$

- B.  $A^3 + A^2 + A I = 0$
- C. Not computable from the given data
- D. 1

65. If A and B are square matrices of the same order, then tr(AB) =

- A. tr(B)tr(A) B. tr(B)+tr(A)
- C. tr(BA) D. tr(B+A)

66. The differential equation 2y dx - (3y - 2x) dy = 0 is

- A. Not exact and homogeneous but not linear
- B. Exact and non-homogeneous but not linear
- C. Exact and homogeneous but linear
- D. Is exact and homogeneous but not linear
- 67. Consider the 2<sup>nd</sup>-order linear equation with constant coefficients : y'' + ay' + y = 0If  $r_1$  and  $r_2$  are the roots of its characteristic equation, then what is  $r_1^2 + r_2^2$ ?
  - A.  $a^2 2b$  B.  $a^2 4b$
  - C.  $a^2 + 2b$  D.  $a^2 + 4b$
- 68. Consider the differential equation : y'' + y = 0. Which of the following is not a solution?
  - A. cos *x* B. tan *x*
  - C.  $\sin x$  D.  $\cos(x+1)$
- 69. The order of a differential equation whose general solution is  $y = A \sin x + B \cos x$ , where A and B are arbitrary constants is

| Α. | 1 | B. | 2 |
|----|---|----|---|
| C. | 3 | D. | 4 |

70. An integrating factor of the differential equation  $\frac{dy}{dx} = \frac{1}{x+y+2}$  is

- A.  $e^y$ B.  $e^{-x}$ C.  $e^{-y}$ D.  $e^x$
- 71. For which value of k is the differential equation  $(x^k + y^k)dx + 2xy dy = 0$  is homogeneous.
  - A. k = 1B. k = 0C. k = 2D.  $k = \frac{1}{2}$

| 72. | lf th<br>valu               | e vector function $V = (x+3y)i + (a+3y)i + (a$ | y – 2  | z)j+(x+az) is solenoidal then the     |
|-----|-----------------------------|--|--------|---------------------------------------|
|     | Α.                          | 0  | В.     | 2                                     |
|     | C.                          | -2   | D.     | 1                                     |
| 73. | The<br><i>F</i> =           | scalar potential of<br>( <i>y</i> + sin z) <i>i</i> + x <i>j</i> + x cos z <i>k</i> is   | the    | conservative vector field             |
|     | Α.                          | ху   | В.     | $xy + \sin z$                         |
|     | C.                          | $x + \sin z$   | D.     | sin z                                 |
| 74. | If $\frac{d}{d}$            | $\frac{du}{dt} = w \times u, \ \frac{dv}{dt} = w \times v, \ \text{then} \ \frac{d}{dt}(u \times v)$   | /)     |                                       |
|     | Α.                          | $w \times (u \times v)$  | В.     | 0                                     |
|     | C.                          | $u \times (w \times v)$  | D.     | $v \times (u \times w)$               |
| 75. | The                         | value of the integral $\int (xdy - ydx)$   | arour  | nd the circle $x^2 + y^2 = 1$ is      |
|     | Α.                          | 0  | В.     | $\pi$                                 |
|     | C.                          | $2\pi$   | D.     | $-2\pi$                               |
| 76. | Whi<br>A.<br>B.<br>C.<br>D. | ch of the following is true about <i>f</i> (a<br>Continuous and differentiable<br>Neither continuous nor differential<br>Continuous but not differentiable<br>Differentiable but not continuous  | z) = z | <sup>2</sup> ?                        |
| 77. | Wha<br>#inc<br>int<br>{     | at will be the output of the following<br>lude <stdio.h><br/>main ()<br/>int y = 10000;<br/>int y = 34;<br/>printf (" Hello World! %d\n", y);<br/>return 0;</stdio.h>  | C co   | de?                                   |
|     | ∫<br>∆                      | Hello World 1000   | R      | Hello Worldt followed by a junk value |
|     | С.                          | Compile time error   | D.     | Hello World! 34                       |
|     |                             |  | -      | -                                     |

78. What will be the final value of *x* in the following C code?

```
#include <stdio.h>
void main ()
{
    int x = 5 * 9 / 3 + 9;
}
A. 3 B. Depends on the compiler
C. 3.75 D. 4
```

79. How many times *i* value is checked in the following C program?#include <stdio . h>

```
80. What will be the output of the following code? #include <stdio . h>
```

```
int main () {
     int a = 3, b = 5;
     int t = a;
     a = b;
     b = t;
     printf("%d %d", a, b);
     return 0;
}
Α.
     55
                                          B.
                                                33
C.
     53
                                           D.
                                                35
```

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```
81. Which of the following is not a keyword in C?
     Α.
          int
                                             Β.
                                                  char
     C.
          include
                                             D.
                                                  str
82. What is the output of the following C code?
     int main ()
     {
     int x = 10;
     printf("%d", x++ + ++x);
     return 0;
     }
     A.
          23
                                             B.
                                                  21
     C.
          22
                                                  20
                                             D.
83. What is the output of this recursive function call?
          int main()
          {
               printf("%d ", factorial(5));
               return 0;
          }
     int factorial (int n)
          {
               if (n==0)
               return 1;
          else
               return n * factorial (n - 1);
          }
          5
                                             Β.
     Α.
                                                  24
     C.
                                                  120
          Error
                                             D.
```

17

84. If a function f(z) is continuous in region *D* and if  $\int_C f(z)dz = 0$ , taken around any simple closed contour *C* in *D*. Then f(z) is A. may or may not be Analytic B. analytic C. not Analytic D. none of these

85. The value of the integral  $\int_C \frac{dz}{z^2 - 2} dz$ , where *C* is the circle |z| = 2 is

 A.  $-\pi i$  B. 0

 C.  $2\pi i$  D.  $\pi i$ 

86. If 
$$z = x + iy$$
, then  $|e^{iz}|$  is equal to  
A.  $e^{-y}$  B. 1

- C.  $e^{y}$  D.  $e^{x^2+y^2}$
- 87. Consider the functions  $f(z) = x^2 + iy^2$  and  $g(z) = x^2 + y^2 + ixy$ . Then which of the following statements are true
  - A. g is analytic but not f B. both f and g are analytic
  - C. f is analytic but not g D. neither f nor g is analytic

88. The coefficient of  $\frac{1}{z}$  in the expansion of  $\log\left(\frac{z}{z+1}\right)$ , |z| > 1 is A. -1 B. 1/2 C. -1/2 D. 1

- 89. If *D* is the open unit disk in  $\mathbb{C}$  and  $f : \mathbb{C} \to D$  is analytic with f(10) = 1/2, then f(10+i) is
  - A. 1/2 B. *i* C. 10+*i* D. -*i*

90. The singular solutions of the differential equation  $y = px + \frac{1}{p}$  are

A.  $\pm 2\sqrt{x}$  B.  $\pm x^2$ 

C. 
$$\pm \sqrt{x}$$
 D. none of these

91. The function  $f(z) = z^2$  maps the first quadrant onto

- A. third quadrant B. itself
- C. right half-plane D. upper half-plane

92. Which of the following is not the real part of the analytic function?

- A.  $1/(x^2 + y^2 + z^2)$ B.  $x^2 - y^2$ C.  $\cos x \cosh y$ D.  $x + x/(x^2 + y^2)$
- 93. The radius of convergence of  $\sum_{n=0}^{\infty} \frac{\left(1+\frac{1}{n}\right)^{n^2}}{n^3}$ A. e B.  $\infty$ C. 1/e D. 0

94. The residue of the function  $f(z) = \frac{1 + e^z}{\sin z + z \cos z}$  at z = 0 is A.  $2\pi i$  B.  $\pi i$ 

95. The value of the integral  $\int_{|z|=2} (x^2 - y^2 + 2ixy) dz$  is

A. *πi*B. 1
C. 0
D. 2*πi*

- 96. The value of the integral  $\int_{|z|=2} \frac{e^{2z}}{(z+1)^4} dz$  is
  - Α. πe Β.  $2\pi e$ C.  $8\pi i/3e^2$ D.  $8\pi e$
- 97. The fixed points of  $f(z) = \frac{z-1}{z+1}$  are
  - Α. 0, 1 1, 2 Β. C. ±1

98. The function  $f(z) = |z|^2$  is

- differentiable everywhere Α.
- differentiable at a countable number of points Β.
- C. differentiable only at z = 0
- D. nowhere differentiable

# 99. If f(z) and $\overline{f(z)}$ are analytic, then

- A. f(z) = zf is a constant function B. C.  $f(z) = z^2$ none of these D.
- 100. The equation  $a_0 x^n + a_1 x^{n-1} + \dots + a_{n-1} x + a_n = 0$  has at least one root between 0 and 1 if

D.

±i

- A.  $\frac{a_1}{n+1} + \frac{a_2}{n} + \ldots + a_n = 0$
- C.  $\frac{a_0}{n+1} + \frac{a_1}{n} + \dots + a_n = 0$

B. 
$$\frac{a_0}{n} + \frac{a_1}{n-1} + \dots + a_n = 0$$

D. None of these

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#### ANSWER SHEET

| 1  | Α | В | С | D | Е |
|----|---|---|---|---|---|
| 2  | Α | В | С | D | Ε |
| 3  | Α | В | С | D | Е |
| 4  | Α | В | С | D | Е |
| 5  | Α | В | С | D | Е |
| 6  | Α | В | С | D | Е |
| 7  | А | В | С | D | Е |
| 8  | А | В | С | D | Е |
| 9  | Α | В | С | D | Е |
| 10 | Α | В | С | D | Е |
| 11 | Α | В | С | D | Е |
| 12 | А | В | С | D | Е |
| 13 | Α | В | С | D | Е |
| 14 | А | В | С | D | Е |
| 15 | Α | В | С | D | Е |
| 16 | Α | В | С | D | Е |
| 17 | Α | В | С | D | Е |
| 18 | А | В | С | D | Е |
| 19 | А | В | С | D | Е |
| 20 | А | В | С | D | Е |
| 21 | Α | В | С | D | Е |
| 22 | Α | В | С | D | Е |
| 23 | Α | В | С | D | Е |
| 24 | Α | В | С | D | Е |
| 25 | Α | В | С | D | Е |

| 26 | А | В | С | D | Е |
|----|---|---|---|---|---|
| 27 | Α | В | С | D | Е |
| 28 | Α | В | С | D | Е |
| 29 | Α | В | С | D | Е |
| 30 | Α | В | С | D | Е |
| 31 | А | В | С | D | Е |
| 32 | А | В | С | D | Е |
| 33 | А | В | С | D | Е |
| 34 | А | В | С | D | Е |
| 35 | А | В | С | D | Е |
| 36 | А | В | С | D | Е |
| 37 | Α | В | С | D | Е |
| 38 | Α | В | С | D | Е |
| 39 | Α | В | С | D | Е |
| 40 | А | В | С | D | Е |
| 41 | Α | В | С | D | Е |
| 42 | Α | В | С | D | Е |
| 43 | А | В | С | D | Е |
| 44 | Α | В | С | D | Е |
| 45 | Α | В | С | D | Е |
| 46 | Α | В | С | D | Е |
| 47 | Α | В | С | D | Е |
| 48 | Α | В | С | D | Е |
| 49 | Α | В | С | D | Е |
| 50 | А | В | С | D | Е |





## **ROUGH WORK**

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