

Code No.

T – 2126

**Entrance Examination for Admission to the P.G. Courses in the  
Teaching Departments, 2024**

**CSS**

**MATHEMATICS / MATHEMATICS WITH  
FINANCE AND COMPUTATION**

**General Instructions**

1. The Question Paper is having 100 Objective Questions, each carrying one mark.
2. The answers are to be (✓) 'tick marked' **only** in the "**Response Sheet**" provided.
3. **Negative marking** : **0.25 marks** will be deducted for each wrong answer .

**Time : 2 Hours**

**Max. Marks : 100**

To be filled in by the Candidate									
Register Number	in Figures								
	in words								

Choose appropriate answer from the options in the questions.

**(100 × 1 = 100 marks)**

1. Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  defined by  $f(x) = \min\{x, x+1, |x-2|\}$ . Then
  - A.  $f$  decreases on the interval  $(-\infty, 1]$
  - B.  $f$  is not continuous on  $\mathbb{R}$
  - C.  $f$  is not differentiable at exactly two points
  - D.  $f$  increases on the interval  $[1, 2]$

DO NOT WRITE HERE

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2. Let  $f : [0,1] \rightarrow \mathbb{R}$  be defined by  $f(x) = \begin{cases} 1 & \text{if } x = 1/4, \\ 2 & \text{if } x = 1/2 \\ 0 & \text{if } x \in [0,1] \setminus \{1/2, 1/4\} \end{cases}$

A.  $f$  is Riemann integrable and  $\int_0^1 f(x) dx = 0$

B.  $f$  is not Riemann integrable

C.  $f$  is Riemann integrable and  $\int_0^1 f(x) dx = 2$

D.  $f$  is Riemann integrable and  $\int_0^1 f(x) dx = 1$

3. Which one of the following does not imply  $a = 0$ ?
- A. for every  $\epsilon > 0, 0 \leq a < \epsilon$                       B. for every  $\epsilon > 0, a < \epsilon$   
C. for every  $\epsilon > 0, 0 \leq a \leq \epsilon$                       D. for every  $\epsilon > 0, -\epsilon < a < \epsilon$
4. An algebraic number is a root of a polynomial whose coefficients are rational. The set of algebraic numbers is
- A. uncountable    B. countably infinite  
C. finite    D. none of these
5. The limit of the sequence  $(\sqrt{(n+1)(n+2)} - n)$  is
- A. 3    B.  $3/2$   
C. 0    D.  $\sqrt{2} - 1$
6. The sequence  $\left(\frac{2^{n+1} + 3^{n+1}}{2^n + 3^n}\right)$  converges to
- A. 0    B. 1  
C. 3    D. 2
7. The value of the integral  $\int_{-\infty}^{\infty} e^{-x^2} dx$  is
- A.  $\sqrt{\pi}$     B.  $2\sqrt{\pi}$   
C. 0    D.  $\sqrt{\pi}/2$
8. If  $\sum a_n = a$  and  $\sum |a_n| = b$ , and  $a$  and  $b$  are finite, then
- A.  $a = b$     B.  $a \leq b$   
C.  $|a| = b$     D.  $a \geq b$
9. If  $x_n = 1 + (-1)^n + \frac{1}{3^n}$ , then
- A.  $\limsup x_n \neq \liminf x_n$                                       B.  $\liminf x_n = -1$   
C.  $x_n$  is a convergent sequence                              D.  $\limsup x_n = 1$

10. Let  $(x_n)$  be a sequence defined by  $x_1 = 2$  and  $x_{n+1} = \frac{1}{2}\left(x_n + \frac{2}{x_n}\right)$ . Then
- A.  $(x_n)$  is an increasing sequence
  - B.  $(x_n)$  converges to  $2\sqrt{2}$
  - C.  $(x_n)$  converges to a rational number
  - D.  $(x_n)$  is a decreasing sequence
11. For  $x \in \mathbb{R}$ , let  $[x]$  denote the greatest integer  $n$  such that  $n \leq x$ . The function  $x[x]$  is
- A. continuous everywhere
  - B. continuous if  $x \in \mathbb{R} \setminus \mathbb{Z}$
  - C. continuous only at  $x = \pm 1, \pm 2, \dots$
  - D. bounded on  $\mathbb{R}$
12. The subset  $A = \{x \in \mathbb{Q} : -1 < x < 0\} \cup \mathbb{N}$  of  $\mathbb{R}$  is
- A. bounded, infinite set and has a limit point in  $\mathbb{R}$
  - B. unbounded, infinite set and has a limit point in  $\mathbb{R}$
  - C. unbounded, infinite set and does not have a limit point in  $\mathbb{R}$
  - D. bounded, infinite set and does not have a limit point in  $\mathbb{R}$
13. The sequence of real-valued functions  $f_n(x) = x^n$ ,  $x \in [0, 1] \cup \{2\}$ , is
- A. uniformly convergent
  - B. not bounded
  - C. pointwise convergent but not uniformly convergent
  - D. bounded but not pointwise convergent











37. Which of the following statements are true?
- A. every group of order 4 is cyclic
  - B. every group of order 6 is abelian
  - C. every subgroup of a cyclic group is cyclic
  - D. every group of order 6 is cyclic
38. The smallest non abelian group is
- A.  $S_3$
  - B. Klein 4 group
  - C.  $D_4$
  - D.  $\mathbb{Z}_4$
39. In the Klein 4 group
- A. order of every element except identity is 2
  - B. order of every element is 2
  - C. order of every element except identity is 3
  - D. order of every element except identity is 4
40. The infinite cyclic group  $\mathbb{Z}$  has exactly
- A. five generators
  - B. two generators
  - C. one generator
  - D. three generators
41. The number of group homomorphisms from  $\mathbb{Z}_{25} \rightarrow \mathbb{Z}$  is
- A. 2
  - B. 3
  - C. 4
  - D. 1
42. The number of ring homomorphisms from  $\mathbb{Z}$  to  $\mathbb{Z}$  is
- A. 2
  - B. 0
  - C. 1
  - D. infinite
43. In a division ring there are exactly
- A. only one idempotent
  - B. two idempotents
  - C. four idempotents
  - D. three idempotents

44. If  $p$  is a prime number,  $x^p + a$  is irreducible over  $\mathbb{Z}_p[x]$
- A. for some values of  $a \in \mathbb{Z}_p$       B. exactly two values of  $a \in \mathbb{Z}_p$   
 C. exactly one value of  $a \in \mathbb{Z}_p$       D. for all  $a \in \mathbb{Z}_p$
45. The polynomial  $f(x) = x^2 + 8x - 2$  is
- A. irreducible over  $\mathbb{Q}$       B. irreducible over  $\mathbb{R}$   
 C. reducible over  $\mathbb{R}$       D. irreducible over  $\mathbb{Q}$  and  $\mathbb{R}$
46. Which of the following statements are true?
- A.  $\{0, 2, 4\}$  is a prime but not a maximal ideal of  $\mathbb{Z}_6$   
 B.  $\{0, 2, 4\}$  is not an ideal of  $\mathbb{Z}_6$   
 C.  $\{0, 2, 4\}$  is a prime and a maximal ideal of  $\mathbb{Z}_6$   
 D.  $\{0, 2, 4\}$  is not a prime but a maximal ideal of  $\mathbb{Z}_6$
47.  $\frac{\mathbb{Z}_3[x]}{\langle x^3 + c \rangle}$  is not a field if
- A.  $c = 2$       B.  $c = 3$   
 C.  $c = 1$       D.  $c = 0$
48. The number of diagonal  $3 \times 3$  complex matrices  $A$  such that  $A^3 = I$  is
- A. 9      B. 27  
 C. 3      D. 1
49. Let  $T: \mathbb{R}^3 \rightarrow \mathbb{R}^3$  be the linear transformation defined by  $T(x_1, x_2, x_3) = (x_1 + x_2, x_2 + x_3, x_3 + x_1)$ . Then an eigenvalue of  $T$  is
- A. 0      B. 3  
 C. 4      D. 2

50. The solutions  $x^2y'' + xy' + 4y = 0$  are
- A.  $\cos(4\log x), \sin(4\log x)$       B.  $\cos(\log x), \sin(\log x)$   
 C.  $\cos(2\log x), \sin(2\log x)$       D.  $\cos(\log x), \sin(2\log x)$
51. An integrating factor of the differential equation  $(y^2x - x^2y)dx + x^3dy = 0$  is
- A.  $(xy)$       B.  $(xy)^{-2}$   
 C.  $(xy)^{-1}$       D.  $(xy)^{-3}$
52. The derivative of the function  $y = \sin^{-1}\left(\sqrt{\frac{x-1}{x+1}}\right) + \sec^{-1}\left(\sqrt{\frac{x+1}{x-1}}\right)$  is
- A. 2      B. 1  
 C. 3      D. 0
53. The distinct eigenvalues of the matrix  $\begin{pmatrix} 1 & 1 & 0 \\ 1 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$  are
- A. 0, -1      B. 1, 2  
 C. 0, 1      D. 0, 2
54. If -1, 2, 3 are the eigenvalues of a  $3 \times 3$  matrix, then its determinant is
- A. 0      B. 4  
 C. -6      D. 6
55. The dimension of the vector space  $\mathbb{R}$  over  $\mathbb{Q}$  is
- A. 0      B. infinite  
 C. 1      D. 2

56. Consider the following subsets of the vector space  $\mathbb{R}^2$ :

$$S1: \{(x, y): x + y \geq 0\}$$

$$S2: \{(x, y): x^2 + y^2 \geq 1\}$$

Which of the following statements are true?

- A.  $S1$  is not a subspace but  $S2$  is a subspace
- B. neither  $S1$  nor  $S2$  is a subspace of  $\mathbb{R}^2$
- C.  $S1$  is a subspace but  $S2$  is not a subspace
- D. both  $S1$  and  $S2$  are subspaces of  $\mathbb{R}^2$

57. If  $V_1$  and  $V_2$  are 3-dimensional subspaces of a 4 dimensional vector space  $V$ , then the smallest possible dimension of  $V_1 \cap V_2$  is

- A. 3
- B. 1
- C. 2
- D. 4

58. Let  $W$  be the vector space of all symmetric matrices over  $\mathbb{R}$ . Then the dimension of  $W$  is

- A. 3
- B. 1
- C. 2
- D. 0

59. The  $10 \times 10$  matrix with all entries 1 have rank

- A. 10
- B. 0
- C. 1
- D. 2

60. A consistent linear system of two equations in two unknowns has

- A. Exactly one solution
- B. Infinitely many solutions
- C. Exactly one solution or an infinite number of solutions
- D. Exactly two solutions

61. Let  $A = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$  be such that  $A$  has real eigenvalues. Then
- A.  $\theta = 0, \frac{-\pi}{2}$                       B.  $\theta = 0, \frac{-3\pi}{2}$
- C.  $\theta = 0, \pi$                       D.  $\theta = 0, \frac{\pi}{2}$
62. A homogeneous system of 5 linear equations in 6 variables admits
- A. Finite, but more than 2 solutions in  $\mathbb{R}^6$
- B. No solution in  $\mathbb{R}^6$
- C. Infinitely many solutions in  $\mathbb{R}^6$
- D. A unique solution in  $\mathbb{R}^6$
63. Suppose the matrix  $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$  has an eigenvalue 1 with associated eigenvector  $x = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$ . What is  $A^{50}x$ ?
- A.  $\begin{bmatrix} 2 \\ 3 \end{bmatrix}$                       B.  $\begin{bmatrix} 2^{50} \\ 3^{50} \end{bmatrix}$
- C.  $\begin{bmatrix} a & b \\ c & d \end{bmatrix}$                       D.  $\begin{bmatrix} a^{50} & b^{50} \\ c^{50} & d^{50} \end{bmatrix}$
64. Given that a  $3 \times 3$  matrix satisfies the equation  $A^3 - A^2 + A - I = 0$ . Then the value of  $A^4$  is
- A.  $-A^3 - A^2 + A - I = 0$
- B.  $A^3 + A^2 + A - I = 0$
- C. Not computable from the given data
- D.  $I$









81. Which of the following is not a keyword in C?

- A. int
- B. char
- C. include
- D. str

82. What is the output of the following C code?

```
int main ()  
{  
int x = 10;  
printf("%d", x++ + ++x);  
return 0;  
}
```

- A. 23
- B. 21
- C. 22
- D. 20

83. What is the output of this recursive function call?

```
int main( )  
{  
    printf("%d ", factorial(5));  
    return 0;  
}  
int factorial (int n)  
{  
    if (n==0)  
        return 1;  
    else  
        return n * factorial (n - 1);  
}
```

- A. 5
- B. 24
- C. Error
- D. 120

84. If a function  $f(z)$  is continuous in region  $D$  and if  $\int_C f(z)dz = 0$ , taken around any simple closed contour  $C$  in  $D$ . Then  $f(z)$  is
- A. may or may not be Analytic      B. analytic  
 C. not Analytic      D. none of these
85. The value of the integral  $\int_C \frac{dz}{z^2 - 2}$ , where  $C$  is the circle  $|z| = 2$  is
- A.  $-\pi i$       B. 0  
 C.  $2\pi i$       D.  $\pi i$
86. If  $z = x + iy$ , then  $|e^{iz}|$  is equal to
- A.  $e^{-y}$       B. 1  
 C.  $e^y$       D.  $e^{x^2+y^2}$
87. Consider the functions  $f(z) = x^2 + iy^2$  and  $g(z) = x^2 + y^2 + ixy$ . Then which of the following statements are true
- A.  $g$  is analytic but not  $f$       B. both  $f$  and  $g$  are analytic  
 C.  $f$  is analytic but not  $g$       D. neither  $f$  nor  $g$  is analytic
88. The coefficient of  $\frac{1}{z}$  in the expansion of  $\log\left(\frac{z}{z+1}\right)$ ,  $|z| > 1$  is
- A.  $-1$       B.  $1/2$   
 C.  $-1/2$       D. 1
89. If  $D$  is the open unit disk in  $\mathbb{C}$  and  $f : \mathbb{C} \rightarrow D$  is analytic with  $f(10) = 1/2$ , then  $f(10+i)$  is
- A.  $1/2$       B.  $i$   
 C.  $10+i$       D.  $-i$





# ANSWER SHEET

1	A	B	C	D	E	26	A	B	C	D	E	51	A	B	C	D	E	76	A	B	C	D	E
2	A	B	C	D	E	27	A	B	C	D	E	52	A	B	C	D	E	77	A	B	C	D	E
3	A	B	C	D	E	28	A	B	C	D	E	53	A	B	C	D	E	78	A	B	C	D	E
4	A	B	C	D	E	29	A	B	C	D	E	54	A	B	C	D	E	79	A	B	C	D	E
5	A	B	C	D	E	30	A	B	C	D	E	55	A	B	C	D	E	80	A	B	C	D	E
6	A	B	C	D	E	31	A	B	C	D	E	56	A	B	C	D	E	81	A	B	C	D	E
7	A	B	C	D	E	32	A	B	C	D	E	57	A	B	C	D	E	82	A	B	C	D	E
8	A	B	C	D	E	33	A	B	C	D	E	58	A	B	C	D	E	83	A	B	C	D	E
9	A	B	C	D	E	34	A	B	C	D	E	59	A	B	C	D	E	84	A	B	C	D	E
10	A	B	C	D	E	35	A	B	C	D	E	60	A	B	C	D	E	85	A	B	C	D	E
11	A	B	C	D	E	36	A	B	C	D	E	61	A	B	C	D	E	86	A	B	C	D	E
12	A	B	C	D	E	37	A	B	C	D	E	62	A	B	C	D	E	87	A	B	C	D	E
13	A	B	C	D	E	38	A	B	C	D	E	63	A	B	C	D	E	88	A	B	C	D	E
14	A	B	C	D	E	39	A	B	C	D	E	64	A	B	C	D	E	89	A	B	C	D	E
15	A	B	C	D	E	40	A	B	C	D	E	65	A	B	C	D	E	90	A	B	C	D	E
16	A	B	C	D	E	41	A	B	C	D	E	66	A	B	C	D	E	91	A	B	C	D	E
17	A	B	C	D	E	42	A	B	C	D	E	67	A	B	C	D	E	92	A	B	C	D	E
18	A	B	C	D	E	43	A	B	C	D	E	68	A	B	C	D	E	93	A	B	C	D	E
19	A	B	C	D	E	44	A	B	C	D	E	69	A	B	C	D	E	94	A	B	C	D	E
20	A	B	C	D	E	45	A	B	C	D	E	70	A	B	C	D	E	95	A	B	C	D	E
21	A	B	C	D	E	46	A	B	C	D	E	71	A	B	C	D	E	96	A	B	C	D	E
22	A	B	C	D	E	47	A	B	C	D	E	72	A	B	C	D	E	97	A	B	C	D	E
23	A	B	C	D	E	48	A	B	C	D	E	73	A	B	C	D	E	98	A	B	C	D	E
24	A	B	C	D	E	49	A	B	C	D	E	74	A	B	C	D	E	99	A	B	C	D	E
25	A	B	C	D	E	50	A	B	C	D	E	75	A	B	C	D	E	100	A	B	C	D	E

## **ROUGH WORK**

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