

Code No.

R – 2117

**Entrance Examination for Admission to the P.G. Courses in the
Teaching Departments, 2023**

CSS

MATHEMATICS/MATHEMATICS WITH FINANCE AND COMPUTATION

General Instructions

1. The Question Paper is having 100 Objective Questions, each carrying one mark.
2. The answers are to be (✓) 'tick marked' **only** in the "**Response Sheet**" provided.
3. **Negative marking** : **0.25 marks** will be deducted for each wrong answer .

Time : 2 Hours**Max. Marks : 100**

To be filled in by the Candidate									
Register Number	in Figures								
	in words								

Choose appropriate answer from the options in the questions.

(100 × 1 = 100 marks)

1. The group $S_3 \times \mathbb{Z}_2$ is isomorphic to which of the following groups?
 - a) \mathbb{Z}_{12}
 - b) A_4 , the alternating group of order 12
 - c) $\mathbb{Z}_6 \times \mathbb{Z}_2$
 - d) D_6 , the dihedral group of order 12

DO NOT WRITE HERE

2. Which of the following rings is a PID?

a) $\mathbb{Q}[X, Y]/\langle X \rangle$

b) $\mathbb{Z} \oplus \mathbb{Z}$

c) $\mathbb{Z}[X]$

d) $M_2(\mathbb{Z})$, the ring of 2×2 matrices with entries in \mathbb{Z}

3. In which of the following fields, the polynomial $x^3 - 312312x + 123123$ is irreducible in $\mathbb{F}[x]$?
- The field \mathbb{F}_3 with 3 elements
 - The field \mathbb{F}_7 with 7 elements
 - The field \mathbb{F}_{13} with 13 elements
 - The field \mathbb{Q} of rational numbers
4. Which of the following are true statements? S_n denotes the symmetric group on n letters, for some $n \geq 1$
- S_n always contains an element of order strictly greater than n
 - If σ_1, σ_2 are elements of order 2, then $\sigma_1\sigma_2$ has order 1 or 2
 - If σ_1, σ_2 are elements of order 3, then $\sigma_1\sigma_2$ has order 1 or 3
 - If $\sigma \in S_n$ has order 3, then σ^2 has order 3
5. Which is one of the following is true?
- $\mathbb{Z}[x]$ is a principal ideal domain
 - $\mathbb{Z}[x]$ is a unique factorization domain
 - $\mathbb{Z}[x]$ is a Euclidean domain
 - $\mathbb{Z}[x]$ is an integral domain, but not a field
6. The number of non-abelian groups of order 8 is
- | | |
|------|------|
| a) 1 | b) 2 |
| c) 4 | d) 5 |
7. Let H be a cyclic subgroup of G of order 32. Then the number of generator of H is
- | | |
|-------|-------|
| a) 4 | b) 8 |
| c) 16 | d) 32 |

8. Let $a = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$, $b = \begin{bmatrix} 0 & 2 \\ \frac{1}{2} & 0 \end{bmatrix} \in GL(2, \mathbb{R})$ and $O(a) = O(b) = 2$. Then $O(ab) =$
 - a) 2
 - b) 4
 - c) 8
 - d) none of these
9. Which of the following is a bilinear transformation?
 - a) $T(z) = i \operatorname{Im}(z)$
 - b) $T(z) = z^3$
 - c) $T(z) = \bar{z}$
 - d) $T(z) = \frac{1}{z}$
10. Which of the following is not true?
 - a) \mathbb{C} is a vector space over \mathbb{R}
 - b) \mathbb{Z} is a vector space over \mathbb{R}
 - c) \mathbb{R} is a vector space over \mathbb{R}
 - d) \mathbb{C} is a vector space over \mathbb{C}
11. A set of single nonzero vector is
 - a) linearly dependent
 - b) linearly independent
 - c) basis
 - d) none of these
12. Which one of the following is not true?
 - a) $\dim_{\mathbb{C}} (\mathbb{C} \times \mathbb{C}) = 2$
 - b) $\dim_{\mathbb{R}} (\mathbb{C}) = 2$
 - c) $\dim_{\mathbb{R}} (\mathbb{C} \times \mathbb{C}) = 2$
 - d) $\dim_{\mathbb{C}} (\mathbb{C}) = 1$
13. Let the linear transformation $T; \mathbb{R}^2 \rightarrow \mathbb{R}^3$ be defined by $T(x_1, x_2) = (x_1, x_1 + x_2, x_2)$ then the nullity of T is
 - a) 0
 - b) 1
 - c) 2
 - d) 3

14. Let n be a positive integer and let $M_n(\mathbb{R})$ denote the space of all $n \times n$ real matrices. If $T : M_n(\mathbb{R}) \rightarrow M_n(\mathbb{R})$ is a linear transformation such that $T(A) = 0$ whenever $A \in M_n(\mathbb{R})$ is symmetric or skew-symmetric, then the rank of T is
 - a) 0
 - b) $\frac{n(n-1)}{2}$
 - c) n
 - d) $\frac{n(n+1)}{2}$
15. The dimension of the vector space of all symmetric matrix $A = (a_{ij})$ of order $n \times n$ ($n \geq 2$) with real entries $a_{11} = 0$ and trace zero is
 - a) $\frac{n^2 + n - 4}{2}$
 - b) $\frac{n^2 - n + 4}{2}$
 - c) $\frac{n^2 + n - 3}{2}$
 - d) $\frac{n^2 - n + 3}{2}$
16. Which of the following is not complete?
 - a) Set of all real numbers \mathbb{R} with usual metric
 - b) Set of all rational numbers \mathbb{Q} with usual metric
 - c) $[0, 1]$ with usual metric
 - d) Any discrete metric space
17. In a discrete metric space, the only connected subsets are
 - a) finite sets
 - b) the whole space
 - c) singleton sets
 - d) all proper subsets
18. Let f be a continuous function defined on \mathbb{R} (with usual metric) into itself and let $A = \{x \in \mathbb{R} : f(x) = 0\}$. Then what best can you say of A ?
 - a) A is closed
 - b) A is open
 - c) A is bounded
 - d) A is compact

19. Which of the following subset of \mathbb{R} with usual metric is neither compact nor connected?
 - a) \mathbb{R}
 - b) $(0, 1)$
 - c) $[0, 100]$
 - d) \mathbb{Q}
20. Which of the following subset is open in with usual metric?
 - a) \mathbb{Q}
 - b) $\left\{1, \frac{1}{2}, \frac{1}{3}, \dots\right\}$
 - c) \mathbb{Z}
 - d) $\mathbb{R} - \mathbb{Z}$
21. Which of the following is not a compact subset of with usual metric?
 - a) $\{x \in \mathbb{R} : x \geq 0\}$
 - b) $[0, 1]$
 - c) $[-1, 1] \cup [-3, -2]$
 - d) any finite subset
22. What is \bar{A} if $A = \left(0, \frac{1}{10}\right)$ in the metric space $M = (0, 1)$ with usual distance metric?
 - a) $\left(0, \frac{1}{10}\right)$
 - b) $\left[0, \frac{1}{10}\right]$
 - c) $\left[0, \frac{1}{10}\right]$
 - d) $\left[0, \frac{1}{10}\right)$
23. Which of the following is true?
 - a) A non-empty subset of a complete metric space is complete
 - b) A non-empty subset of a compact metric space is compact
 - c) A non-empty subset of a totally bounded set is totally bounded
 - d) A non-empty subset of a connected metric space is connected
24. Which of the following is a convergent series?
 - a) $\sum_{n=1}^{\infty} \frac{1}{(\log n)^n}$
 - b) $\sum_{n=1}^{\infty} \frac{1}{n(\log n)}$
 - c) $\sum_{n=1}^{\infty} \frac{1}{n(\log n)^{\frac{1}{2}}}$
 - d) $\sum_{n=2}^{\infty} \frac{1}{\log n}$

25. Let (a_n) be given by $a_1 = \sqrt{2}$ and $a_{n+1} = \sqrt{2a_n}$ for all $n \geq 1$. Then $\lim_{n \rightarrow \infty} a_n$ is
 - a) $\sqrt{2}$
 - b) 2
 - c) 1
 - d) ∞
26. If $p \neq 0, \beta$ are real and $\alpha\bar{\alpha} - p\beta \geq 0$, then the equation $pz\bar{z} + \alpha\bar{z} + \bar{\alpha}z + \beta = 0$ represents.
 - a) real axis
 - b) a straight line
 - c) a circle
 - d) imaginary axis
27. The number of limit points of the sequence $\{1, 2, 3, 4, 5, 1, 2, 3, 4, 5, 1, 2, 3, 4, 5, \dots\}$ is
 - a) 2
 - b) 3
 - c) 5
 - d) 10
28. What values of x for which the function $x^3 - 3x^2 + 6$ is decreasing?
 - a) $x = 0$
 - b) $x < 2$
 - c) $x > 2$
 - d) $x > 3$
29. The envelope of the family of curves $Pt^2 + Qt + R = 0$, where t is a parameter, is
 - a) $Q^2 = 4PR$
 - b) $R = 2PQ$
 - c) $Q = 4PR$
 - d) $R^2 = 4PQ$
30. The number of evolutes for a curve is
 - a) always one
 - b) always finite
 - c) always infinite
 - d) none of these
31. The number of asymptotes parallel to the x -axis for the curve $x^2y^2 = c^2(x^2 + y^2)$ is
 - a) one
 - b) two
 - c) three
 - d) either two or three

38. If the projections of a line on the X, Y, Z axes are 2, 6, 3 respectively, then the length of the line is
 - a) 49
 - b) 7
 - c) 11
 - d) 14
39. A surface generated by a line which is always parallel to a fixed line in space is generally called a
 - a) cylinder
 - b) right circular cone
 - c) cone
 - d) right circular cylinder
40. The direction cosines of a plane parallel to the plane $X = 0$ are proportional to (here c is any constant)
 - a) 0, 0, c
 - b) 0, c , 0
 - c) c , 0, 0
 - d) c , c , 0
41. The equation of the plane, making intercepts p, q, r on the coordinate axes OX, OY, OZ respectively, is
 - a) $px + qy + rz = 0$
 - b) $px + qy + rz = 1$
 - c) $\frac{p}{x} + \frac{q}{y} + \frac{r}{z} = 1$
 - d) $\frac{x}{p} + \frac{y}{q} + \frac{z}{r} = 1$
42. The equation $x^2 + y^2 + z^2 + x - y - z + 1 = 0$, $x - y - z + 1 = 0$ taken together represents a
 - a) sphere
 - b) plane
 - c) cone
 - d) circle
43. The residue of $\frac{ze^z}{(z-1)^3}$ at its pole is
 - a) $\frac{e}{2}$
 - b) $\frac{3e}{4}$
 - c) $\frac{3e}{2}$
 - d) $\frac{e}{4}$

44. The radius of convergence of the series $\sum_{n=1}^{\infty} \frac{z^n}{n^2}$ is
- a) e
- b) $\frac{1}{e}$
- c) 1
- d) 5
45. The conjugate of a complex number is $\frac{1}{i-1}$. Then that complex number is
- a) $\frac{-1}{i-1}$
- b) $\frac{1}{i+1}$
- c) $\frac{-1}{i+1}$
- d) $\frac{1}{i-1}$
46. Let $f(z) = e^{\frac{1}{z}}$. Then
- a) f is analytic at $z = 0$
- b) f has simple pole at $z = 0$
- c) f has removable singularity at $z = 0$
- d) f has essential singularity at $z = 0$
47. Let $f(z) = \frac{z^2}{z+2}$. Then the maximum value of $|f(z)|$ in $\{z \in \mathbb{C}: |z| \leq 1\}$ is
- a) $1/3$
- b) 1
- c) $3/2$
- d) 2
48. Which of the following function is differentiable only at $z = 0$?
- a) $f(z) = \operatorname{Re} z$
- b) $f(z) = \operatorname{Im} z$
- c) $f(z) = \bar{z}$
- d) $f(z) = |z|^2$

49. The residue of $\frac{(z^2 - 2z)}{(z+1)^2(z^2 + 4)}$ at $z = 2i$ is
- a) $\frac{7+i}{25}$ b) $\frac{7-i}{25}$
- c) $\frac{-14}{25}$ d) $\frac{14}{25}$
50. The region of convergence of the power series $\sum_{n=1}^{\infty} nz^{n-1}$ is
- a) $1 < |z| < 2$ b) $|z| < 1$
- c) $|z| < 2$ d) $2 < |z|$
51. The solution of a partial differential equation $2p + 3q = 1$ is
- a) $\phi(3x + 2y, y + 3z) = 0$ b) $\phi(3x + 2y, y - 3z) = 0$
- c) $\phi(3x - 2y, y + 3z) = 0$ d) $\phi(3x - 2y, y - 3z) = 0$
52. The differential equation of all spheres whose centres lie on the z-axis is
- a) $p = q$ b) $py = qx$
- c) $px = qy$ d) $z = px + qy$
53. The solution of the differential equation $(x^2 + 1)\frac{dy}{dx} + (y^2 + 1) = 0$ is
- a) $y = 2 + x^2$ b) $y = \frac{x+1}{1-x}$
- c) $y = x(x-1)$ d) $y = \frac{1-x}{1+x}$
54. The particular integral of $(D-5)(D-4)y = 1000$ is
- a) -50 b) 100
- c) -100 d) 50

61. The value of $\iint_A dx dy$, where A is a rectangle with vertices $(-2, -1)$, $(2, -1)$, $(2, 1)$ and $(-2, 1)$ is
 - a) 2
 - b) 4
 - c) 6
 - d) 8
62. The integral value $\int_{x=0}^1 \int_{y=x^2}^x f(x, y) dy dx$ is equivalent to
 - a) $\int_{y=x^2}^x \int_{x=0}^1 f(x, y) dx dy$
 - b) $\int_{y=0}^1 \int_{x=y}^{\sqrt{y}} f(x, y) dx dy$
 - c) $\int_{y=0}^1 \int_{x=y^2}^y f(x, y) dx dy$
 - d) $\int_{y=0}^1 \int_{x=\sqrt{y}}^{y^2} f(x, y) dx dy$
63. The value of $\int_C (3x + y) dx + (2y - x) dy$ along the straight line C joining from $(0, 5)$ to $(2, 5)$ is
 - a) 4
 - b) 8
 - c) 16
 - d) 32
64. The _____ statement when executed in a switch statement causes immediate exit from the structure.
 - a) goto
 - b) default
 - c) break
 - d) if..else
65. The largest value that an unsigned char type variable can store is
 - a) 32767
 - b) 127
 - c) 65535
 - d) 255

66. In an exit-controlled loop, if the body is executed n times, then how many times test condition is evaluated?
 - a) $n + 2$
 - b) $n + 1$
 - c) n
 - d) $n - 1$
67. The function _____ does not require any conversion specification to read a string from the keyboard.
 - a) scanf()
 - b) strcmp()
 - c) strcpy()
 - d) getchar()
68. A variable declared inside a function by default assumes _____ storage class.
 - a) register
 - b) auto
 - c) static
 - d) external
69. If $p1$ and $p2$ are both pointers to the same array, which one of the following statements is incorrect?
 - a) $p1 == p2$
 - b) $*p2 / *p1$
 - c) $p2 - p1$
 - d) $p2 + p1$
70. What is the high level I/O function to write a set of data values to a file?
 - a) printf()
 - b) putw()
 - c) putc()
 - d) fprintf()
71. Which of the following is an invalid variable name?
 - a) constant1
 - b) 1var
 - c) total
 - d) sum value

72. Let $f : [a, b] \rightarrow \mathbb{R}$ be an integrable function. Define $g : [a, b] \rightarrow \mathbb{R}$ by $g(x) = \int_x^b f(t) dt$ then
- a) g is not differentiable b) $g'(x) = f(x)$
c) $g'(x) = -f(x)$ d) $g'(x) = g(x) + f(x)$
73. Let D be a non-zero $n \times n$ real matrix with $n \geq 2$. Which of the following implications is valid?
- a) $\det(D) = 0$ implies $\text{rank}(D) = 0$ b) $\det(D) = 1$ implies $\text{rank}(D) \neq 1$
c) $\text{rank}(D) = 1$ implies $\det(D) \neq 0$ d) $\text{rank}(D) = n$ implies $\det(D) \neq 1$
74. The value of $\int_{-1}^1 |x| dx$ is
- a) 0 b) -1
c) 1 d) $\frac{1}{2}$
75. Let $(x_n) \rightarrow x$ and (y_n) be a sequence such that $|y_n| \leq M$, for all n . Then the sequence $(x_n y_n)$ converges if
- a) $x < 0$ b) $x > 0$
c) $x = 0$ d) $x = M$
76. Let (a_n) be a bounded real sequence. Then (a_n) converges if
- a) It is a Cauchy sequence b) it must be a constant sequence
c) it must be monotone d) it has a convergent subsequence

77. Let (a_n) be a real sequence such that $|a_n - a_{(n+1)}| \rightarrow 0$ as $n \rightarrow \infty$. Then
- a) (a_n) converges
 - b) (a_n) is bounded
 - c) $(|a_n|)$ converges
 - d) (a_n) need not be convergent
78. Let $a_1 = 8$ and $a_{(n+1)} = \frac{a_n}{2} + 2$, for all n . Suppose that $(a_n) \rightarrow a$. Then the value of a is
- a) $1/4$
 - b) 4
 - c) $1/8$
 - d) 8
79. Let $a_n = \frac{n}{(n^2 + 1)} + \frac{n}{(n^2 + 2)} + \dots + \frac{n}{(n^2 + n)}$, $\forall n$. Then (a_n) is
- a) a convergent sequence
 - b) a bounded sequence but not convergent
 - c) an unbounded sequence but not diverges to $+\infty$
 - d) a divergent sequence diverges to $+\infty$
80. For which of the following curves the curvature is constant at every point on the curve?
- a) Parabola
 - b) Ellipse
 - c) Circle
 - d) Cycloid
81. Let $f(x) = 2x^3 - 9x^2 + 12x - 11$. Then f attains
- a) local maximum at $x = 1$ and local minimum at $x = 2$
 - b) local minimum at $x = 1$ and local minimum at $x = 2$
 - c) local maximum at both $x = 1$ and $x = 2$
 - d) local minimum at both $x = 1$ and $x = 2$

87. Which of the following series is not convergent?

a) $\sum_{n=1}^{\infty} \frac{1}{n}$

b) $\sum_{n=1}^{\infty} \frac{1}{n!}$

c) $\sum_{n=1}^{\infty} \frac{1}{n^3}$

d) $\sum_{n=1}^{\infty} \frac{1}{n^4}$

88. The unit normal vector of the surface $xyz = 1$ at the point $(1, 1, 1)$ is

a) $i + j + k$

b) $(i + j + k)/2$

c) $(i + j + k)/\sqrt{2}$

d) $(i + j + k)/\sqrt{3}$

89. The value of k for which $C_1 + kC_2$ is perpendicular to C_3 , where $C_1 = i + 2j + 3k$, $C_2 = i + 2j + k$ and $C_3 = 3i + j$, is

a) 3

b) 4

c) 5

d) 6

90. If the angle between two non-zero vectors is greater than $\frac{\pi}{2}$ and smallest than $\frac{3\pi}{2}$, then the dot product of these vectors is

a) zero

b) greater than zero

c) less than zero

d) not defined

91. The Laplace transform of $\int_0^t \int_0^t \int_0^t (t \sin t) dt dt dt$ is

a) $\frac{2}{s^2(s^2 + 1)^2}$

b) $\frac{2}{s^2(s + 1)}$

c) $\frac{2}{s(s + 1)^2}$

d) $\frac{2}{s^2(s^2 + 1)}$

92. The Laplace transform of $\frac{t^5}{e^{2t}}$ is

a) $\frac{6!}{(s+2)^5}$

b) $\frac{5!}{(s+2)^6}$

c) $\frac{5!}{(s-2)^6}$

d) $\frac{6!}{(s-2)^5}$

93. The Laplace transform of $\sin^2 t$ is

a) $\frac{1}{2s} + \frac{s}{2s^2 + 8}$

b) $\frac{1}{s} + \frac{s}{2s^2 + 4}$

c) $\frac{1}{s} - \frac{s}{s^2 + 4}$

d) $\frac{1}{2s} - \frac{s}{2s^2 + 8}$

94. The inverse Laplace transform of $\frac{s}{(2s^2 - 8)}$ is

a) $\frac{1}{2} \sinh 2t$

b) $\frac{1}{2} \cosh 2t$

c) $\frac{1}{2} \cos 2t$

d) $\frac{1}{2} \sin 2t$

95. The inverse Laplace transform of $\frac{s}{(s+2)^2}$ is

a) $e^{-2t}(1+t)$

b) $e^{-2t}(1+2t)$

c) $e^{-2t}(1-2t)$

d) $e^{-2t}(1-t)$

ANSWER SHEET

1	A	B	C	D	E
2	A	B	C	D	E
3	A	B	C	D	E
4	A	B	C	D	E
5	A	B	C	D	E
6	A	B	C	D	E
7	A	B	C	D	E
8	A	B	C	D	E
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94	A	B	C	D	E
95	A	B	C	D	E
96	A	B	C	D	E
97	A	B	C	D	E
98	A	B	C	D	E
99	A	B	C	D	E
100	A	B	C	D	E

ROUGH WORK

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